## **Common and Natural Logarithms**

### **Common Logarithms**

- A common logarithm has a <u>base of 10</u>.
- If there is no base given explicitly, it is common.
- You can easily find common logs of powers of ten.
- You can use your calculator to evaluate common logs.

#### **Natural Logarithms**

- A natural logarithm has a <u>base of e</u>.
- We write natural logarithms as <u>ln</u>.
  - o In other words,  $\log_{e}(1) = \ln(1)$
- If  $\ln e = x$ ,  $\log_e e = x$   $e^x = e^x$   $e^x = e^1$  x = 1  $\ln e = 1$

#### The Number e

- The mathematical constant e is the unique real number such that the value of the derivative (the slope of the tangent line) of the function  $f(x) = e^x$  at the point x = 0 is exactly 1.
- The function e<sup>x</sup> so defined is called the exponential function.
- The inverse of the exponential function is the natural logarithm, or logarithm with base e.
- The number *e* is also commonly defined as the base of the natural logarithm (using an integral to define the latter), as the limit of a certain sequence, or as the sum of a certain series.
- The number e is one of the most important numbers in mathematics, alongside the additive and multiplicative identities 0 and 1, the constant  $\pi$ , and the imaginary number i.
- *e* is irrational, and as such its value cannot be given exactly as a finite or eventually repeating decimal. The numerical value of *e* truncated to 20 decimal places is:

# **Change of Base Formula**

- Allows us to convert to a different base.
- If a, b, and n are positive numbers and neither a nor b is 1, then the following equation is true.

$$\log_a n = \frac{\log_b n}{\log_b a}$$

## **Examples**